

## **Chapter 17 Time Series**

**Proof** that  $F_{t+1} = \alpha A_t + \alpha(1-\alpha)A_{t-1} + \alpha(1-\alpha)^2 A_{t-2} + \dots$  can be written as  
 $F_{t+1} = F_t + \alpha E_t$

$F_{t+1} = \alpha A_t + \alpha(1-\alpha)A_{t-1} + \alpha(1-\alpha)^2 A_{t-2} + \dots$  can be written as

$$F_{t+1} = \alpha A_t + (1-\alpha)[\alpha A_{t-1} + \alpha(1-\alpha)A_{t-2} + \dots]$$

$$F_{t+1} = \alpha A_t + (1-\alpha)F_t$$

$$F_{t+1} = \alpha A_t + F_t - \alpha F_t$$

$$F_{t+1} = F_t + \alpha(A_t - F_t)$$

The difference between the actual and forecast in the last bracketed term is the error in period t.

$$F_{t+1} = F_t + \alpha E_t$$